Data and Research Question

We analyze artificial earthquake data derived from large-scale computer simulations based on a 1994 earthquake in Northridge (USA). In each of 135 simulations, the (isotropic) absolute ground velocity [m/s] was measured at 6146 virtual seismograms with a temporal resolution of 2Hz.

This project marks the first time that physics-based simulations of earthquakes are combined with modern statistical methods. Apart from gaining new insights in the geophysical processes regression models could in future be used to predict expected ground movements in earthquake regions.

Main research question

How do the physical conditions at an earthquake fault affect the surficial ground velocity measured over time?

Challenges

- Very high-dimensional data
- Spatio-temporal functional data
- Predicted ground velocity
- Absolute ground velocity by dynamic coefficient of friction
- Hypocentral distance
- Elevation of seismometer [m]
- Moment magnitude [N/m]
- Dynamic coefficient of friction
- Direction of tectonic background stress [°]
- Categorization into landforms performed using the Topographic Position Index (TPI) of Weiss (2001)

Setting

The artificial earthquake data were generated using the open-source software SeisSol (www.seissol.org). In each simulation:

1. Five [simulation parameters] were pre-set, and
2. Absolute ground velocities were simulated solving elastic wave equations coupled to frictional failure at the earthquake fault.

Simulation setup

The artificial earthquake data were generated using the open-source software SeisSol (www.seissol.org). In each simulation:

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Influence parameters

The influence parameters are all constant over time.

- Soil material ([rock, sediment])
- Linear slip weakening distance [m]
- Static coefficient of friction
- Dynamic coefficient of friction
- Hypocentral distance of seismometer [m]
- Elevation of seismometer [m]
- Landform at seismometer ([ridge, plain, valley, ...])
- Moment magnitude [N/m]
- Categorization into landforms performed using the Topographic Position Index (TPI) of Weiss (2001)

Figure 1: Left: Categorized mean absolute ground velocity in one simulation over the area under study, darker colours correspond to increased velocity. Right: Typical observations of absolute ground velocity over time. The initial peak of the ground velocity is delayed and smaller as hypocentral distance increases.

1. Modeling process

We use a Generalized Functional Additive Model (GFAM) (see Scheipl et al., 2016) which is an extension of the GAM model class.

In our case, only the response is functional and we use a Gamma model with log-link.

\[
y(t) \sim F(\mu(t), \nu) \quad \text{with} \quad g(\mu(t)) = \beta_0(t) + \sum_i \beta_i(X_i, t), \quad i = 1, \ldots, n
\]

- \(y(t)\): Value of functional response observed at time point \(t\)
- \(F(\mu(t), \nu)\): Conditional distribution of \(y(t)\) with conditional expectation \(\mu(t)\) and shape parameters \(\nu\)
- \(g(\cdot)\): Link function
- \(\beta_i(X_i, t)\): Functional intercept
- \(\beta_i(X_i, t)\): One of \(R\) additive effects with associated covariates \(X_i\) and potentially varying over the functional time domain \(t\)
- \(n\): number of functional observations

We use a highly performant estimation algorithm from Wood et al. (2016) to make estimation of this complex model on such large data feasible. Major advances are:

- a block-wise Cholesky decomposition
- a compressed representation of marginal spline bases

A prediction error based approach was used for tuning basis sizes, resulting smooth effects were estimated using (tensor product) P-splines.

2. Covariate effects

The hypocentral distance and the dynamic frictional resistance have by far the strongest effects, with higher values leading to decreased ground velocities for both.

3. Model evaluation

Figure 3: From left to right: Residuals vs fitted values, residuals vs the time domain, residuals vs space, autocovariance of residuals over the functional domain. The black dot in the third plot marks the epicenter.

4. Conclusion & Outlook

Functional additive regression models are a promising approach for modeling surficial ground velocity.

- Our model allows a better understanding of the observed seismological patterns
- Our model adds value to the current seismological discussion of how important precise determination of specific physical parameters is
- Our model offers predictions which could in future replace computer-intensive earthquake simulations

Secondary finding

Moment magnitude can be predicted very well using the simulation parameters (98.2% explained null deviance).

Future research

The model will be refined further, e.g. by explicitly modeling spatial correlation and by relaxing the strict assumption of the hypocenter as fixed point source for all earthquakes. Furthermore model performance will be examined for additional earthquakes.

References


